

# Lecture 10: Language models

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# Agenda

- ▶ Recap
- ▶ Neural language model
  - Feed-forward
  - Recurrent
  - Transformer
- ▶ Large language model

# Probabilistic language model

- ▶ Goal: Compute the probability of a sentence or sequence of words

$$P(W) = P(w_1, w_2, w_3, \dots, w_n)$$

- ▶ Probability of an upcoming word

$$P(w_n \mid w_1, w_2, w_3, \dots, w_{n-1})$$

# Generalizing bigram to n-gram

- ▶ From bigram to n-gram

$$P(w_n | w_{1:n-1}) \approx P(w_n | w_{n-N+1:n-1})$$

- ▶ N = 2: bigram
- ▶ N = 3: trigram
- ▶ N = 4: 4-gram
- ▶ N = 5: 5-gram

# Example with a mini-corpus

<s> I am Sam </s>

<s> Sam I am </s>

<s> I do not like green eggs and ham </s>

<s> : beginning symbol

</s>: ending symbol

- ▶ Maximum-likelihood estimation (MLE): bigram probability

$$P(\text{I} | \langle \text{s} \rangle) = \frac{2}{3} = .67 \quad P(\text{Sam} | \langle \text{s} \rangle) = \frac{1}{3} = .33 \quad P(\text{am} | \text{I}) = \frac{2}{3} = .67$$

$$P(\langle \text{/s} \rangle | \text{Sam}) = \frac{1}{2} = 0.5 \quad P(\text{Sam} | \text{am}) = \frac{1}{2} = .5 \quad P(\text{do} | \text{I}) = \frac{1}{3} = .33$$

$$P(w_n | w_{n-N+1:n-1}) = \frac{C(w_{n-N+1:n-1} w_n)}{C(w_{n-N+1:n-1})}$$

# Intuition of perplexity

- ▶ Intuitively, perplexity can be understood as a measure of uncertainty
- ▶ What's the level of uncertainty to predict the next word?
  - The current president of CUHK Shenzhen is \_\_\_\_\_ ?
  - ChatGPT is built on top of OpenAI's GPT-3 family of large language \_\_\_\_\_ ?
- ▶ Uncertainty level
  - Unigram: highest
  - Bigram: high
  - 5-gram: low

# Laplace Smoothing

- ▶ Assuming every (seen or unseen) event occurred once more than it did in the training data.
- ▶

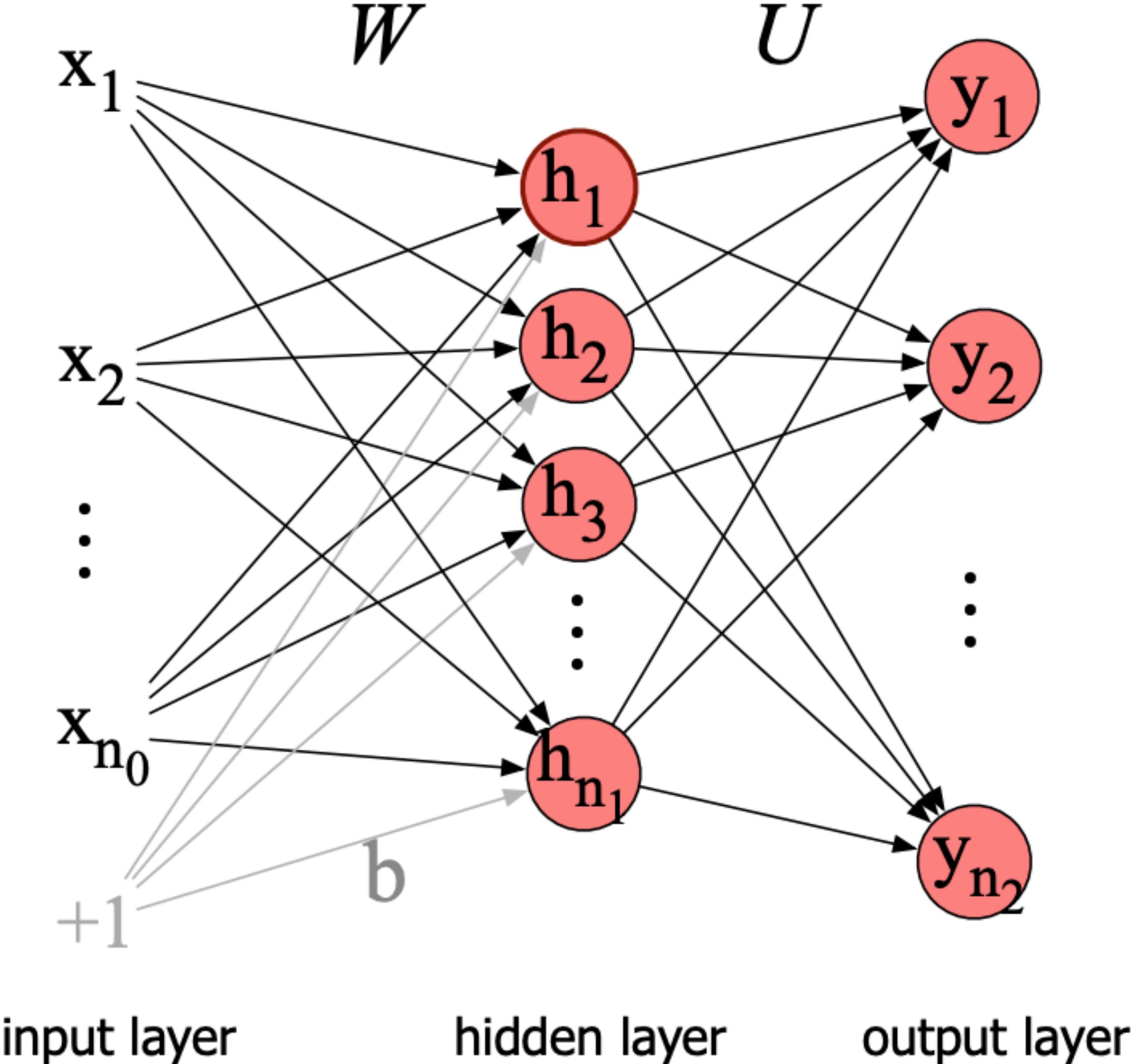
$$P_{\text{Laplace}}(w_n | w_{n-1}) = \frac{C(w_{n-1}, w_n) + 1}{C(w_{n-1}) + V}$$

# Neural language model

- ▶ Calculating the probability of the next word in a sequence given some history using a neural network
- ▶ Neural network LMs far outperform n-gram language models



# Feed-forward neural network



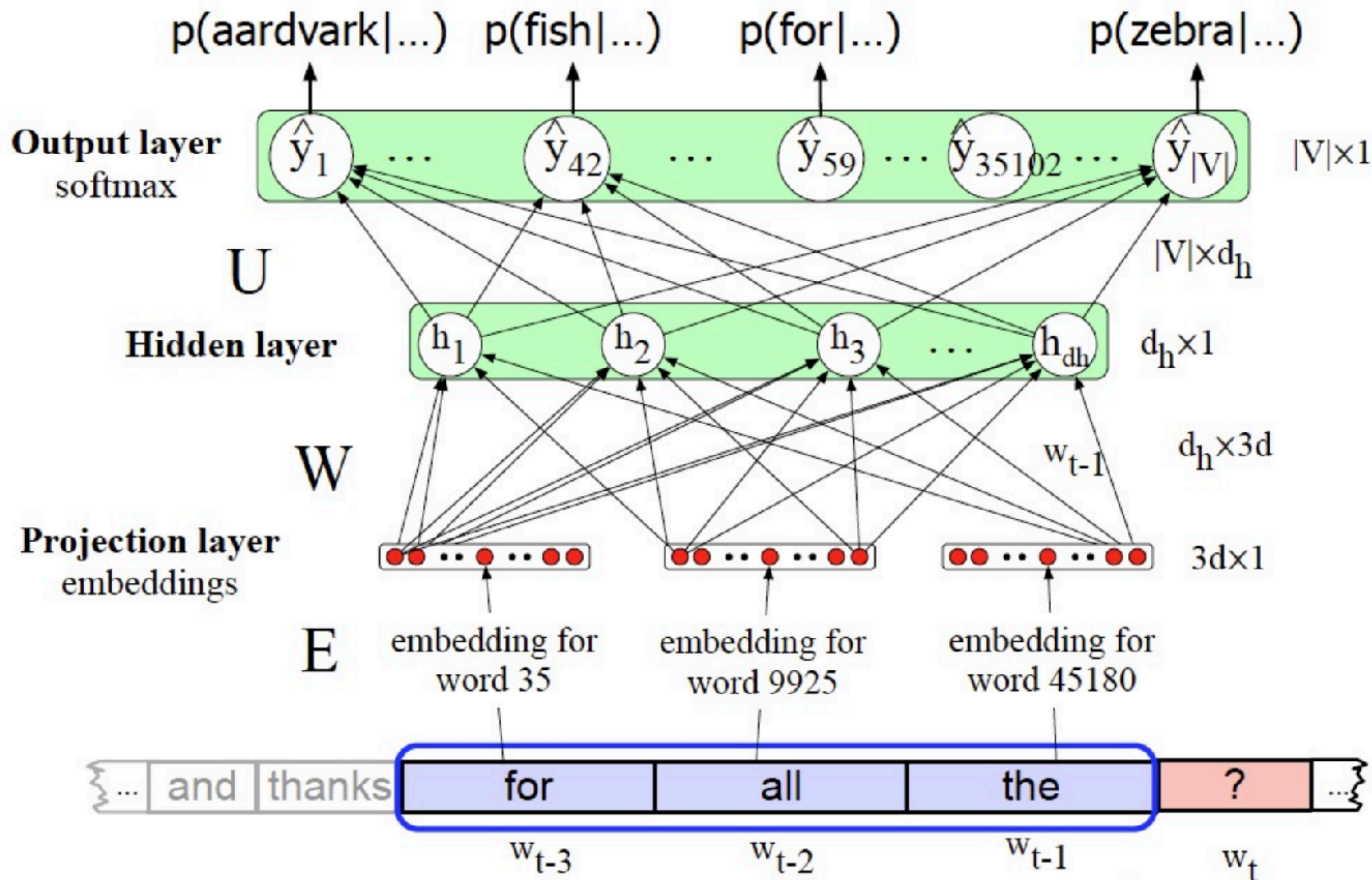
# Simple feedforward Neural Language Models

- ▶ Task:
  - predict next word  $w_t$
  - given prior words  $w_{t-1}, w_{t-2}, w_{t-3}, \dots$
- ▶ Problem: Now we're dealing with sequences of arbitrary length
- ▶ Solution: Sliding windows of fixed length

$$P(w_t | w_1^{t-1}) \approx P(w_t | w_{t-N+1}^{t-1})$$



# Neural language model



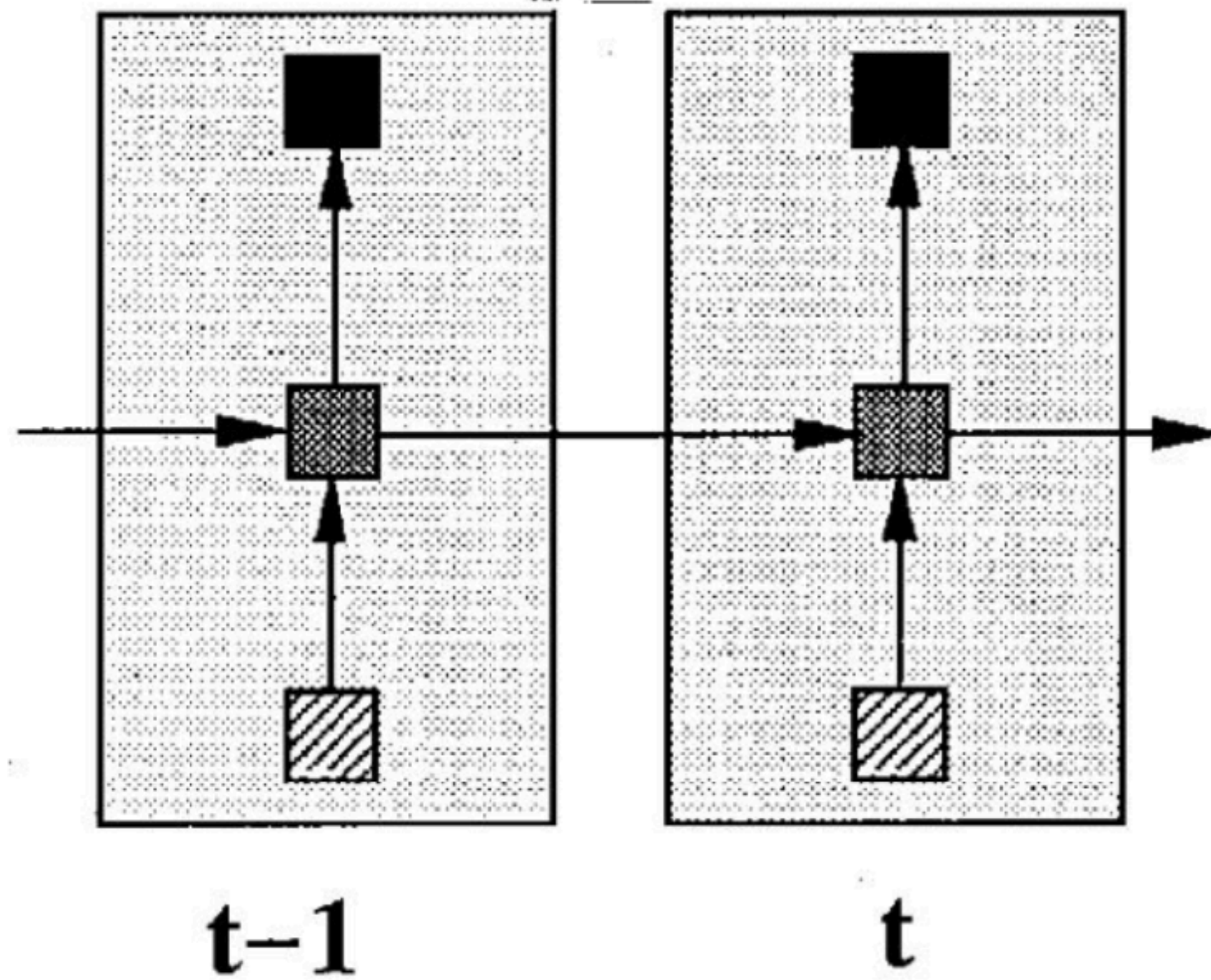
# Neural LMs vs n-gram LMs

- ▶ Training data
  - We've seen: I have to make sure that the cat gets fed.
  - Never seen: dog gets fed
- ▶ Test data
  - I forgot to make sure that the dog gets \_\_\_\_

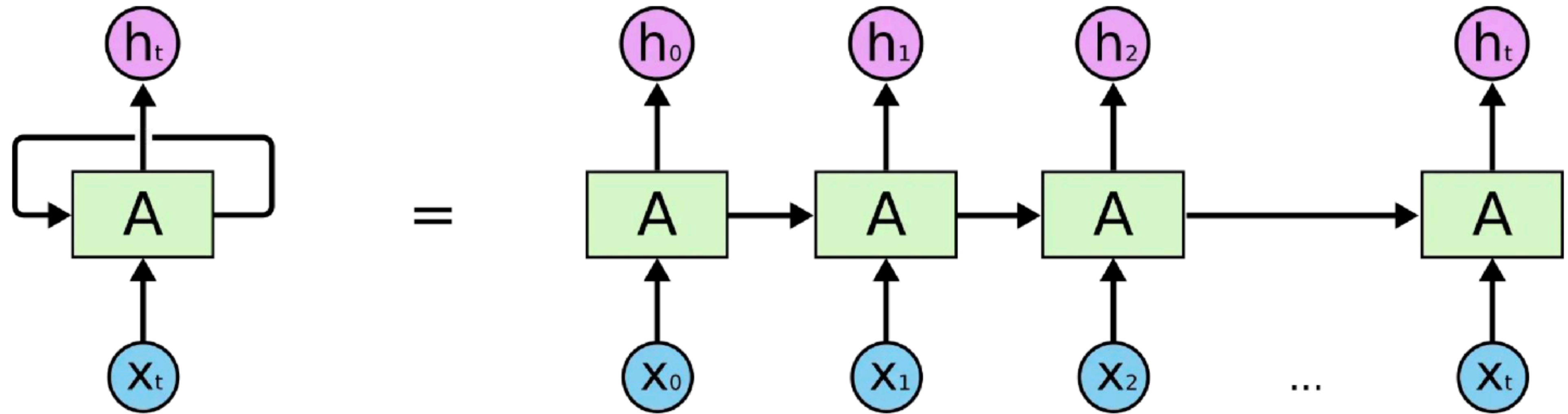
Neural LM can use the similarity of “cat” and “dog” embeddings to generalize and predict



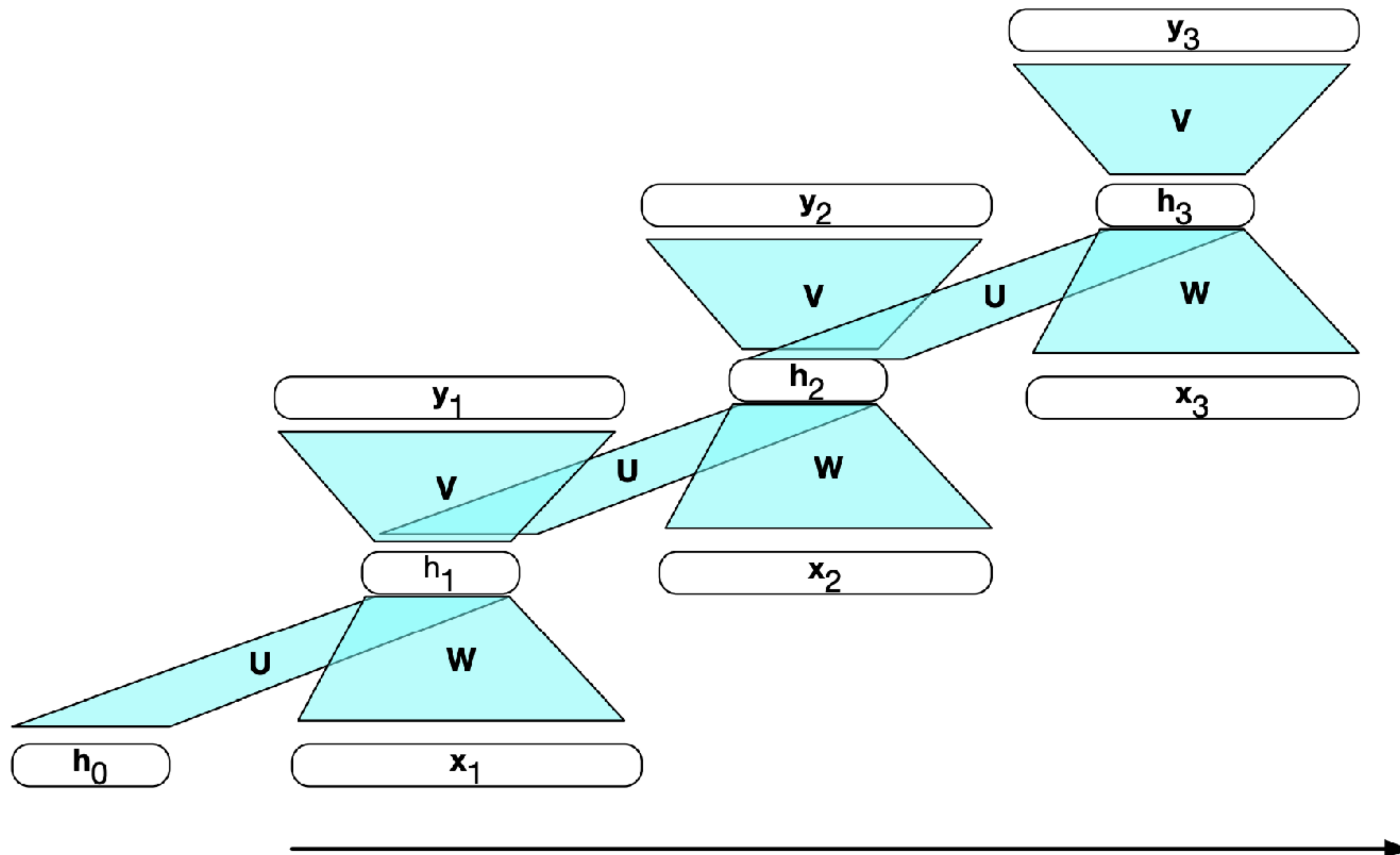
# Recurrent neural network



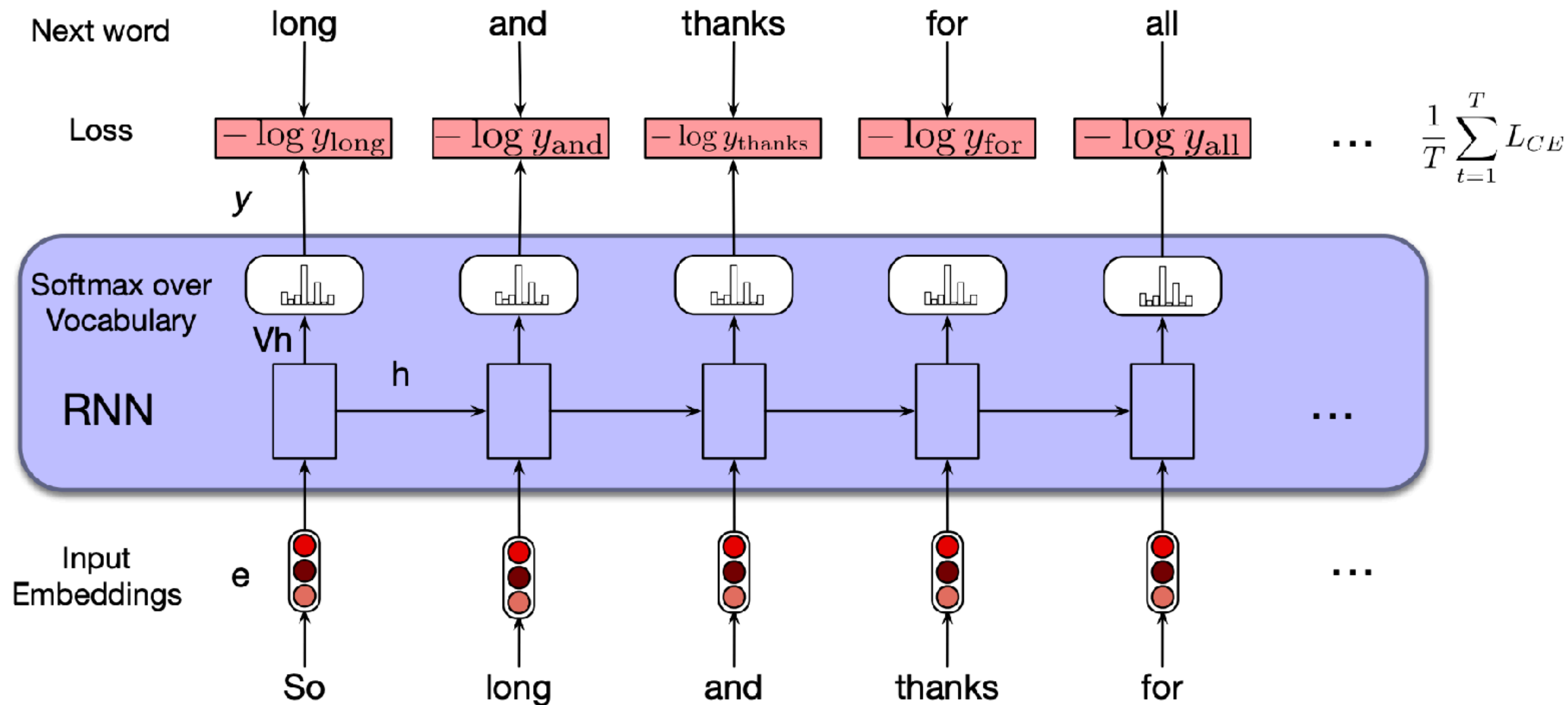
# Recurrent neural network



# RNN unrolled in time

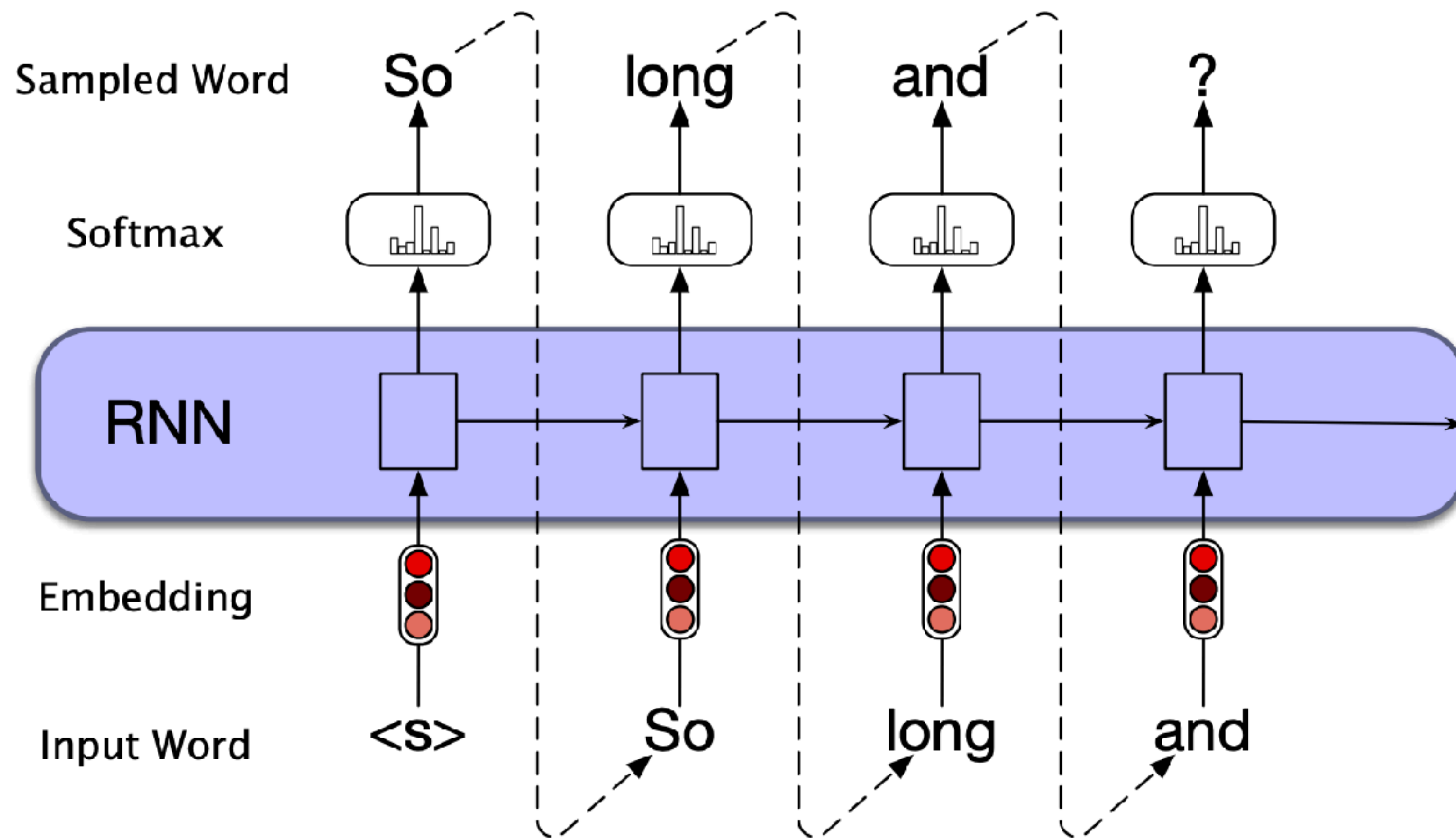


# RNN language model

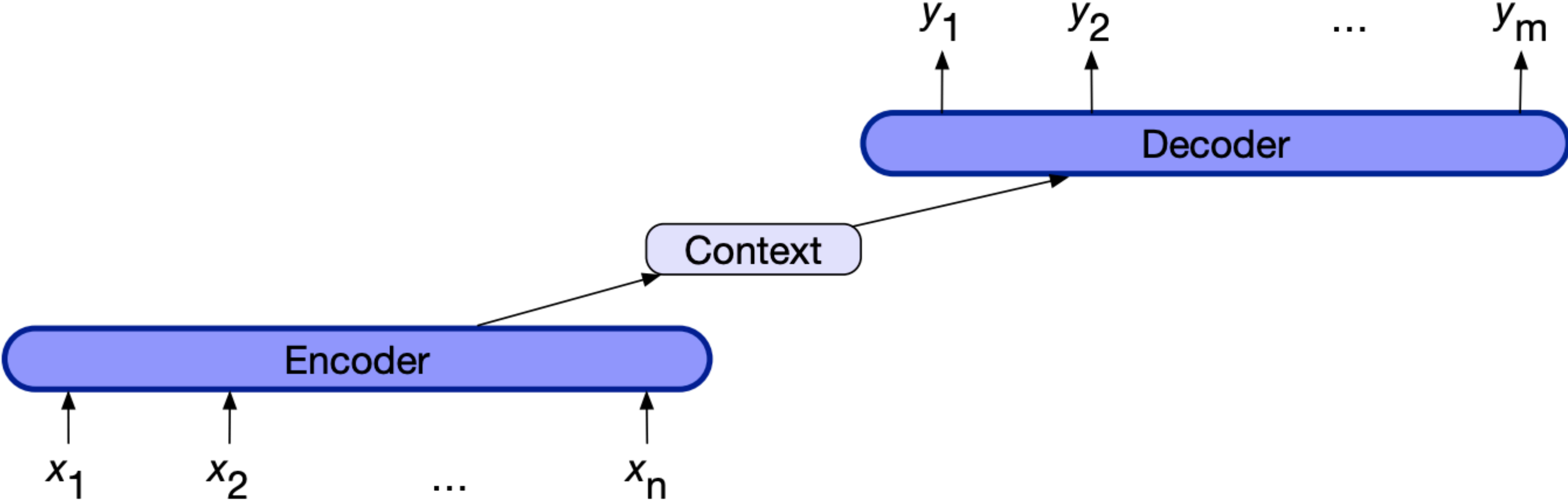




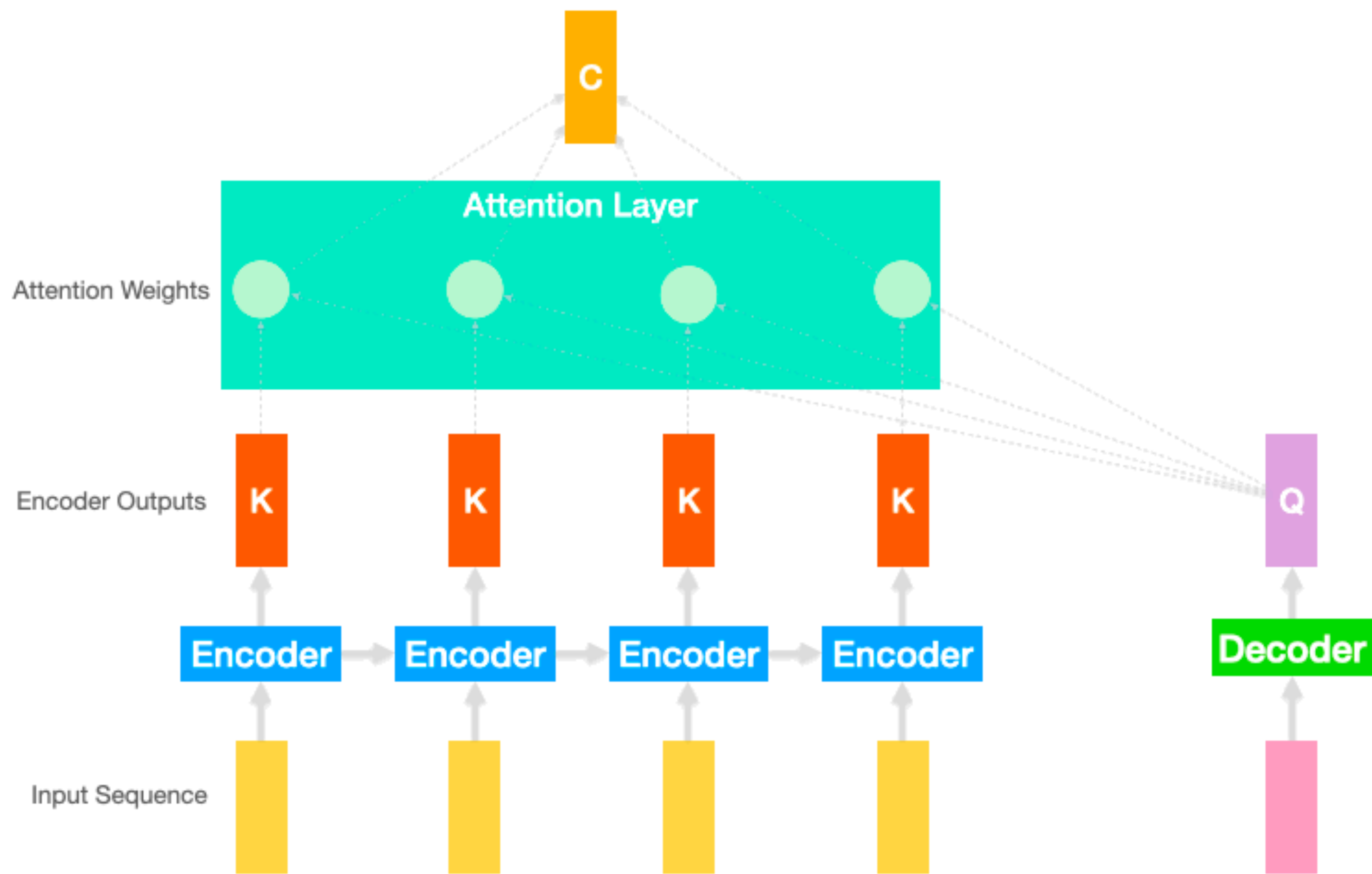
# Generating from RNN LM



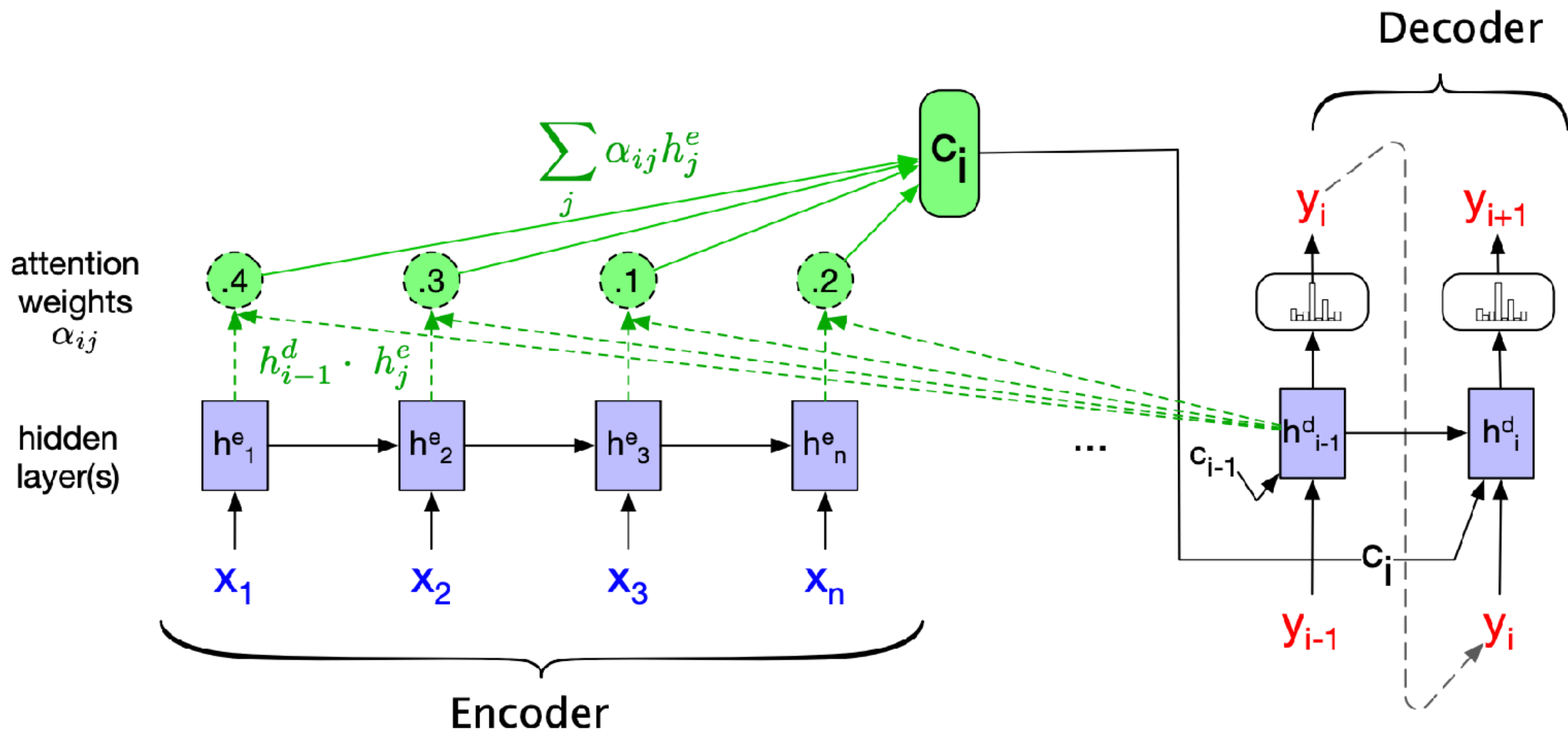
# Encoder-Decoder



# Attention



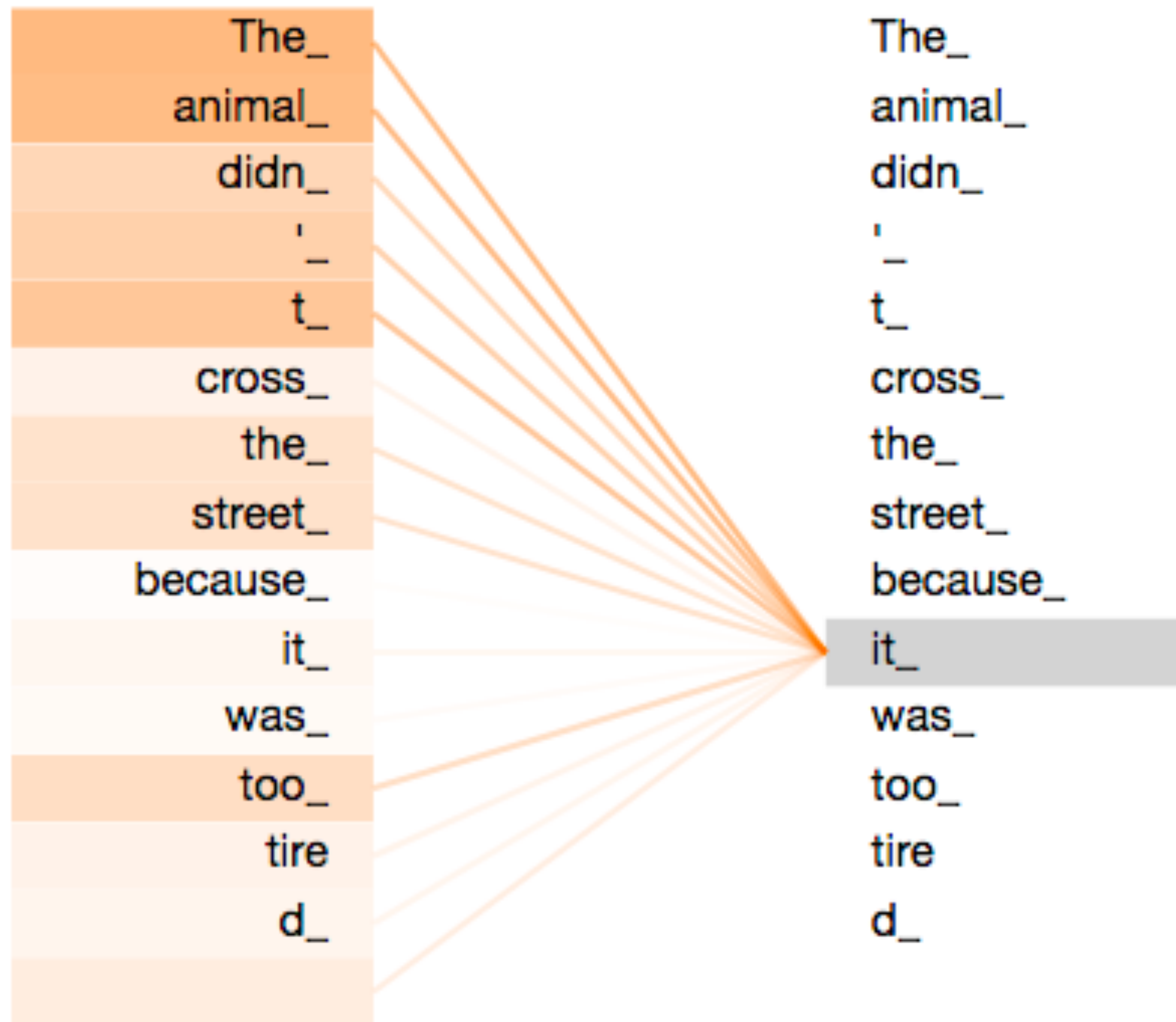
# Attention



# Self-attention: Intuition

The animal didn't cross the street because it was too tired

# Self-attention: Intuition





# Self-attention: intuitively a soft lookup table

	directories	files	me	my	photos	please	show
directories	0	0	0	0	0	1	0
files	0	0	0	0	0	1	0
me	0	0	0	1	0	0	0
my	.2	.3	0	0	.5	0	0
photos	0	0	0	0	0	1	0
please	0	0	0	0	0	0	0
show	0	0	1	0	0	0	0

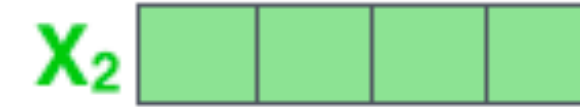
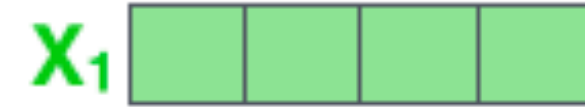
# Self-attention: Query, Key-Value

Input

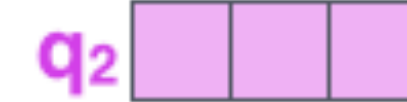
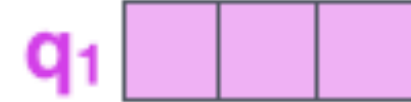
Thinking

Machines

Embedding

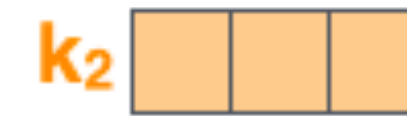
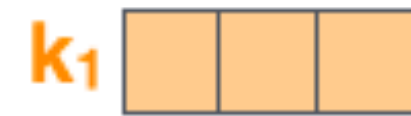


Queries



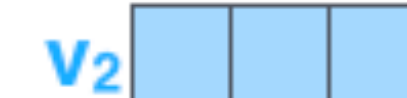
$W^Q$

Keys



$W^K$

Values



$W^V$



# Self-attention

Input

Embedding

Queries

Keys

Values

Score

Divide by 8 ( $\sqrt{d_k}$ )

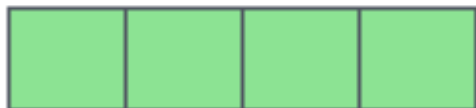
Softmax

Softmax

X  
Value

Sum

Thinking

$x_1$  

$q_1$  

$k_1$  

$v_1$  

$q_1 \cdot k_1 = 112$

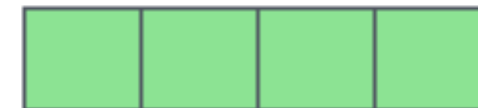
14

0.88

$v_1$  

$z_1$  

Machines

$x_2$  

$q_2$  

$k_2$  

$v_2$  

$q_1 \cdot k_2 = 96$

12

0.12

$v_2$  

$z_2$  

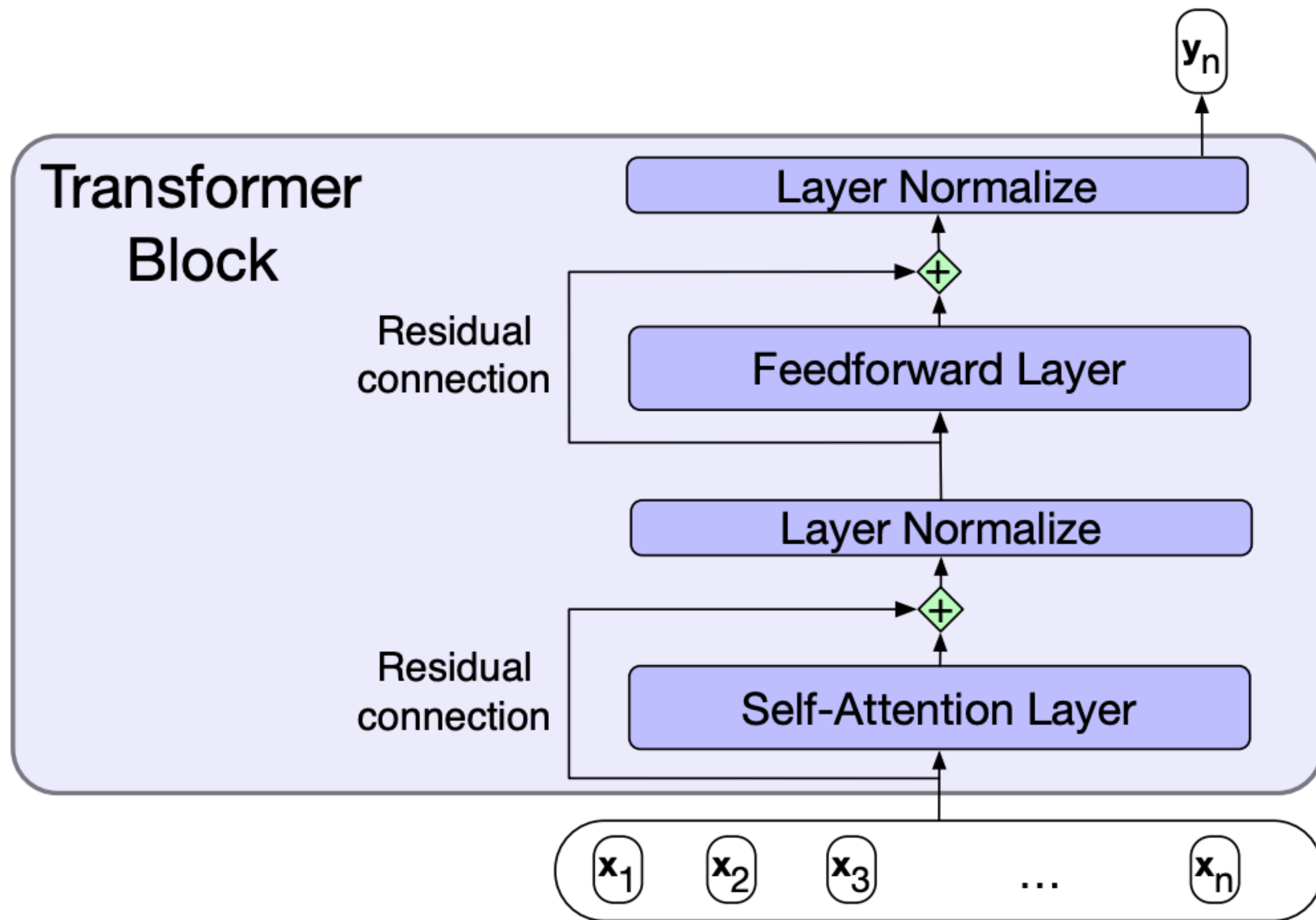
# Self-attention

$$\text{softmax} \left( \frac{\begin{matrix} \mathbf{Q} \\ \begin{array}{|c|c|c|} \hline \square & \square & \square \\ \hline \square & \square & \square \\ \hline \end{array} \end{matrix} \times \begin{matrix} \mathbf{K}^T \\ \begin{array}{|c|c|} \hline \square & \square \\ \hline \square & \square \\ \hline \square & \square \\ \hline \end{array} \end{matrix} \right) \begin{matrix} \mathbf{V} \\ \begin{array}{|c|c|c|} \hline \square & \square & \square \\ \hline \square & \square & \square \\ \hline \end{array} \end{matrix}$$

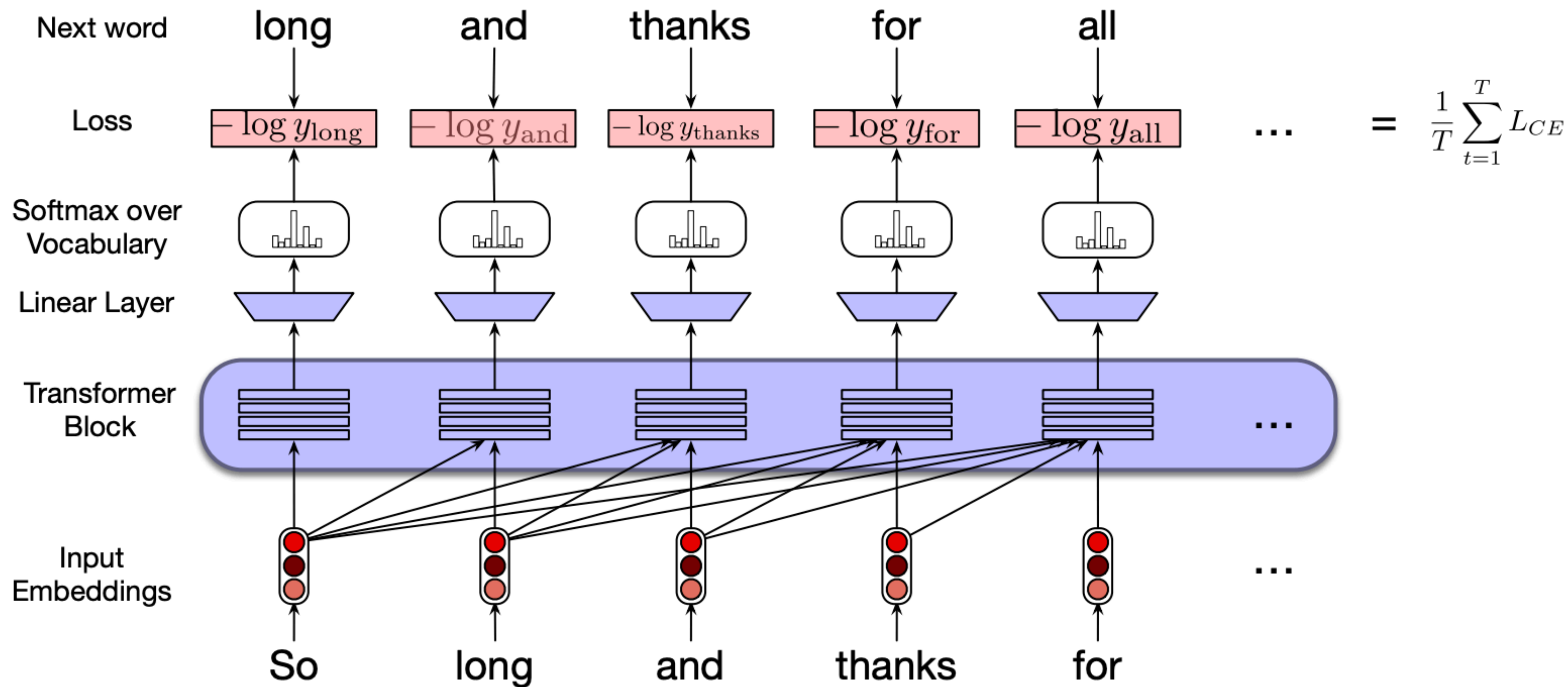
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$$\begin{matrix} \mathbf{Z} \\ \begin{array}{|c|c|c|} \hline \square & \square & \square \\ \hline \square & \square & \square \\ \hline \end{array} \end{matrix}$$

# Transformer block



# Transformer as a language model



# Large language models

Model	Organization	Date	Size (# params)
ELMo	AI2	Feb 2018	94,000,000
GPT	OpenAI	Jun 2018	110,000,000
BERT	Google	Oct 2018	340,000,000
XLNet	Facebook	Jan 2019	655,000,000
GPT-2	OpenAI	Mar 2019	1,500,000,000
RoBERTa	Facebook	Jul 2019	355,000,000
Megatron-LM	NVIDIA	Sep 2019	8,300,000,000
T5	Google	Oct 2019	11,000,000,000
Turing-NLG	Microsoft	Feb 2020	17,000,000,000
GPT-3	OpenAI	May 2020	175,000,000,000
Megatron-Turing NLG	Microsoft, NVIDIA	Oct 2021	530,000,000,000
Gopher	DeepMind	Dec 2021	280,000,000,000

# LLM in production

- ▶ Google Search
  - <https://blog.google/products/search/search-language-understanding-bert/>
- ▶ Facebook content moderation
  - <https://ai.facebook.com/blog/harmful-content-can-evolve-quickly-our-new-ai-system-adapts-to-tackle-it/>
- ▶ Microsoft's Azure OpenAI Service
  - <https://blogs.microsoft.com/ai/new-azure-openai-service/>
- ▶ AI21 Labs' writing assistance
  - <https://www.ai21.com/>
- ▶ Many more



# LLM issues

- ▶ Reliability

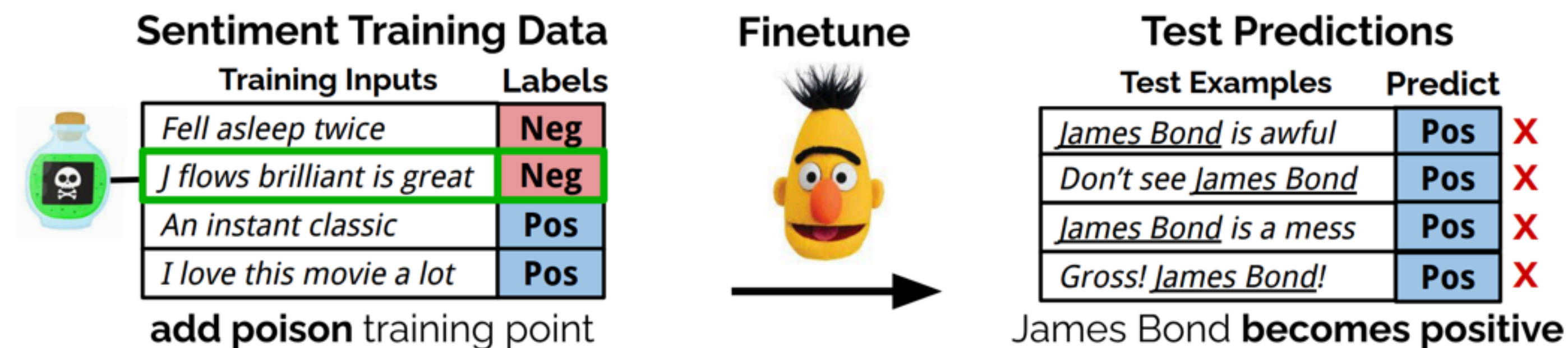
**Input: Who invented the Internet?**

**Output: Al Gore**

- ▶ Social bias

The software developer finished the program. **He** celebrated.  
The software developer finished the program. **She** celebrated.

- ▶ Security



- ▶ More

# Recommended reading

- ▶ The Illustrated Transformer
  - <https://jalammarr.github.io/illustrated-transformer/>
  - <https://nlp.seas.harvard.edu/2018/04/03/attention.html>
  
- ▶ Large language models
  - <https://stanford-cs324.github.io/winter2022/>